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x_1 x_2 , 0, .1; "0" (".")
 $y = x_1 \wedge x_2 = x_1 \cdot x_2 = x_1 x_2$, (1), 0,
 x_1 x_2 , 0, .1;
 $y = x$ - ,
 (1), (0),
 (. .1).

1

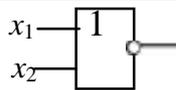
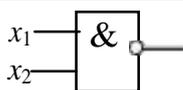
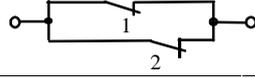
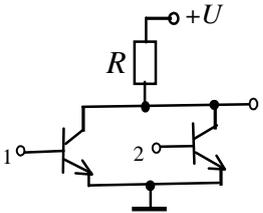
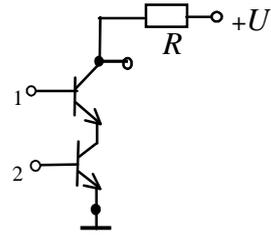
	\vee +	\wedge ил	\bar{x}																																		
	$y = x_1 \vee x_2 = x_1 + x_2$	$y = x_1 \wedge x_2 = x_1 x_2$	$y = \bar{x}$																																		
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(), () () -
 $y \wedge x_1 < x_2$, $y \wedge x_1 x_2$ $y = x$ -
 $y \wedge x_1 \bar{x}_2 < x_1 x_2 \bar{x}_2$
 1 $1 \neq 2$ 0 $1 = 2 = 0$ $1 = 2 = 1, \dots$
 $y \wedge x_1 \beta x_2$.

3.

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 ↓ ()
 $x_1 = 1, x_2 = 0: y = x_1 \downarrow x_2 = x_1 + x_2$;
 $x_1 = 1, x_2 = 1: y = x_1 x_2 = x_1 x_2$.

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	a	b	c	3
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

.3, : $y(a, b, c) = \bar{a}bc + a\bar{b}c + abc + \bar{a}\bar{b}c.$

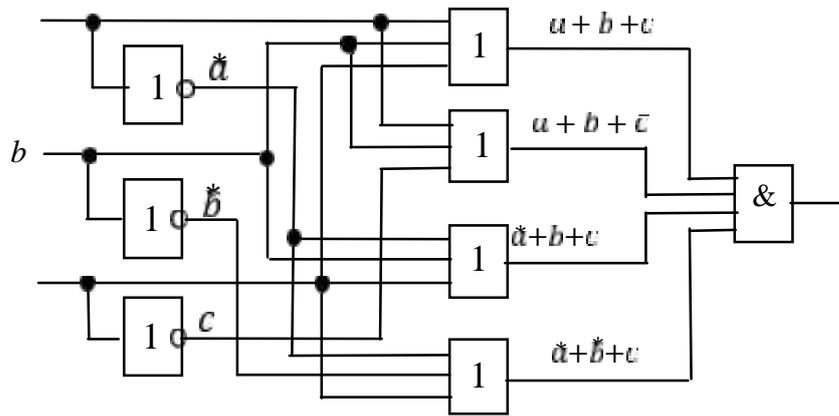
(.3)

$$y(a, b, c) = (a + b + c)(a + b + \bar{c})(a + \bar{b} + c)(a + \bar{b} + \bar{c}).$$

5.

$$y = (a + b + c)(a + b + \bar{c})(\bar{a} + b + c)(\bar{a} + \bar{b} + c).$$

(.1).



. 1.

3.

1.	$y \in a + b(\bar{c} + d) + (c + a\bar{d})$
2.	$y \in a + d(\bar{c} + d) + (b + a)(a + c)$
3.	$y \in (a + b)(c + d) + (c + a\bar{b})$
4.	$y \in (a + b)(\bar{c} + d)(c + \bar{d}) + (d + a)$
5.	$y \in a + b(\bar{c} + d) + (c + a)(d + b)$
6.	$y \in a + b + d(\bar{c} + d) + (c + a\bar{d})$
7.	$y \in a + d + d(\bar{c} + d) + (b + a)(a + c)$
8.	$y \in (a + b + d)(c + d) + (c + a\bar{b})$
9.	$y \in (a + b + d)(\bar{c} + d)(c + \bar{d}) + (d + a)$
10.	$y \in a + b + d(\bar{c} + d) + (c + a)(d + b)$
11.	$y \in a + b + d(\bar{c} + d) + (c + a\bar{d})$
12.	$y \in a + d + d(\bar{c} + d) + (b + a)(a + c)$
13.	$y \in (a + b + d)(c + d) + (c + a\bar{b})$
14.	$y \in (a + b + d)(\bar{c} + d)(c + \bar{d}) + (d + a)$
15.	$y \in b + d(\bar{c} + d) + (c + a)(d + b)$
16.	$y \in b + d(\bar{c} + d) + (c + a\bar{d})$
17.	$y \in d + d(\bar{c} + d) + (b + a)(a + c)$
18.	$y \in (b + d)(c + d) + (c + a\bar{b})$
19.	$y \in (b + d)(\bar{c} + d)(c + \bar{d}) + (d + a)$
20.	$y \in b + d(\bar{c} + d) + (c + a)(d + b)$
21.	$y \in d + b + d(\bar{c} + d) + (c + a\bar{d})$
22.	$y \in d + d + d(\bar{c} + d) + (b + a)(a + c)$
23.	$y \in (d + b + d)(c + d) + (c + a\bar{b})$
24.	$y \in (d + b + d)(\bar{c} + d)(c + \bar{d}) + (d + a)$
25.	$y \in (d + b + d)(c + d) + (c + a\bar{b})$

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" " 1 2,
 $y \overline{N}x_1 \overline{x_2} < x_1 x_2^-$ $y \overline{N}x_1 x_2$ $\overline{N}x_1 < x_2$
 $y \overline{N}x_1 \beta x_2$ $y \overline{N}x_1 < x_2$ $\overline{N}x_1 x_2$

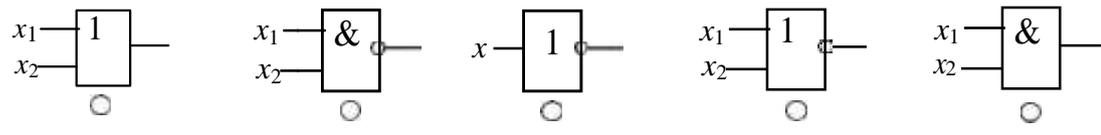
3.

" " 1 2,
 $y \overline{N}x_1 \overline{x_2} < x_1 x_2^-$ $y \overline{N}x_1 x_2$ $y \overline{N}x_1 \beta x_2$
 $\overline{N}x_1 < x_2$ $y \overline{N}x_1 < x_2$ $\overline{N}x_1 x_2$

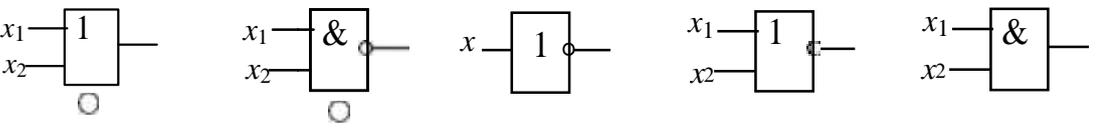
4.

().
 $y(a, b, c) = \overline{a}bc + a\overline{b}c + abc + \overline{a}\overline{b}c$
 $y(a, b, c) \overline{N}(\overline{b} < c)(a < \overline{b} < \overline{c})(a < \overline{b} < c)(a < \overline{b} < c)$
 $y(a, b, c) \overline{N}(\overline{a}b < c < \overline{a}bc)(abc < \overline{a}b < c)$

5.



6.

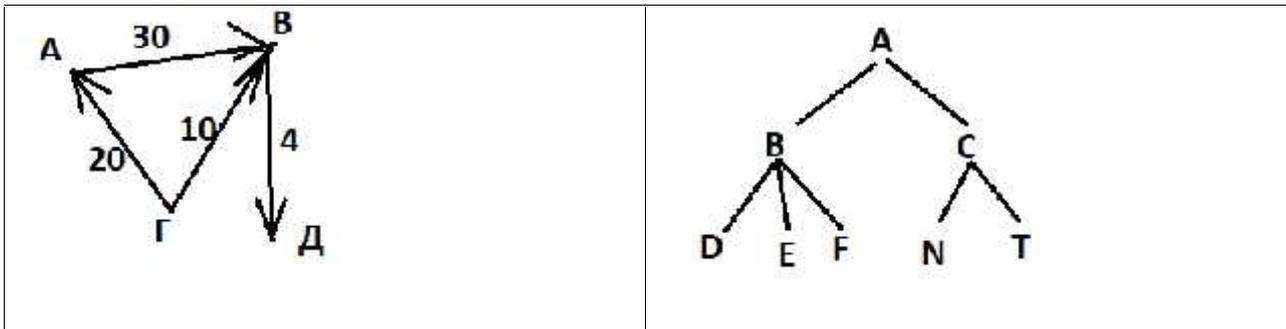


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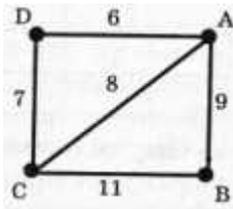
<p>1)</p>	<p>2)</p>
<p>3)</p> <p>()</p>	<p>4)</p> <p>()</p>



1.

A,

B, C, D



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1) 11;

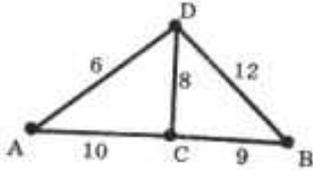
2) 15;

3) 18;

4) 20.

2.

A, B, C, D



(

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1) 12;

2) 16;

3) 18;

4) 19.

5.

1) ABCD

AB=9 AC=8 AD=6 BC=11 BD=15 CD=7

2) -15

: 2

6.

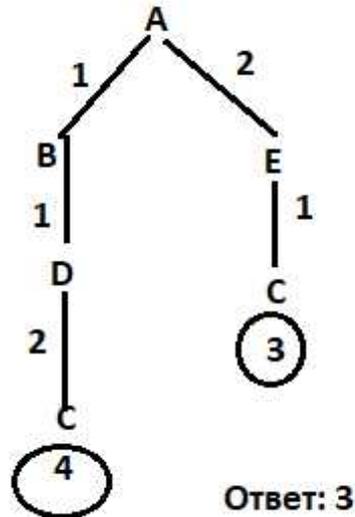
1) ABCD

AB=18 AC=10 AD=6 BC=9 BD=12 CD=8

2) -18

: 3

Запись в тетради:



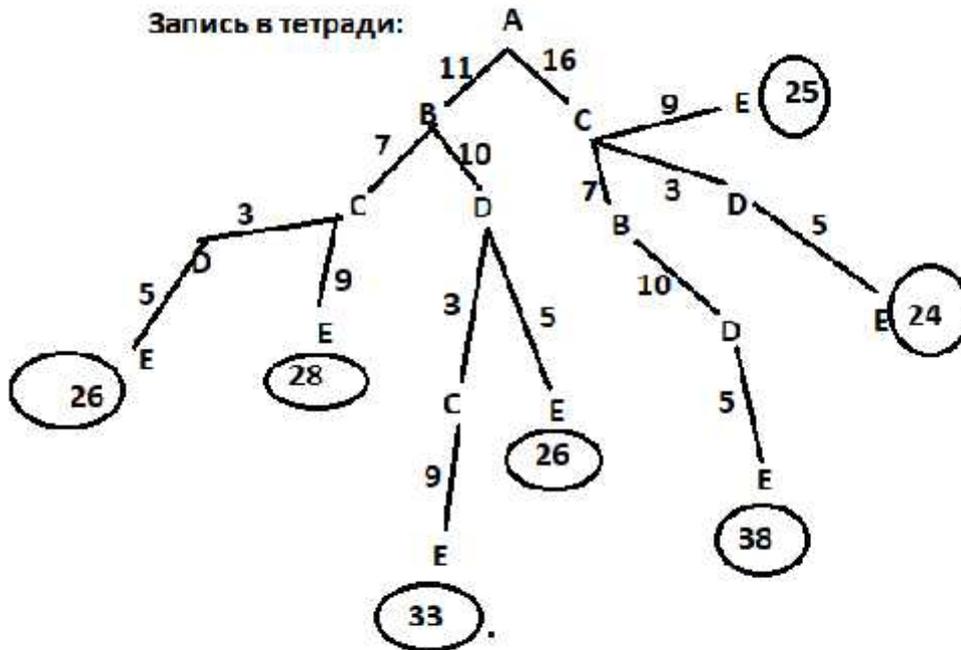
9) Между населёнными пунктами А, В, С, D и Е построены дороги, протяжённость которых приведена в таблице. (Прочерк в таблице означает, что прямой дороги между пунктами нет.)

	А	В	С	D	Е
А	-	11	16	-	-
В	11	-	7	10	-
С	16	7	-	3	9
D	-	10	3	-	5
Е	-	-	9	5	-

Определите длину кратчайшего пути между пунктами А и Е (при условии, что передвигаться можно только по построенным дорогам).

- 1) 20 2) 24 3) 25 4) 26

Запись в тетради:

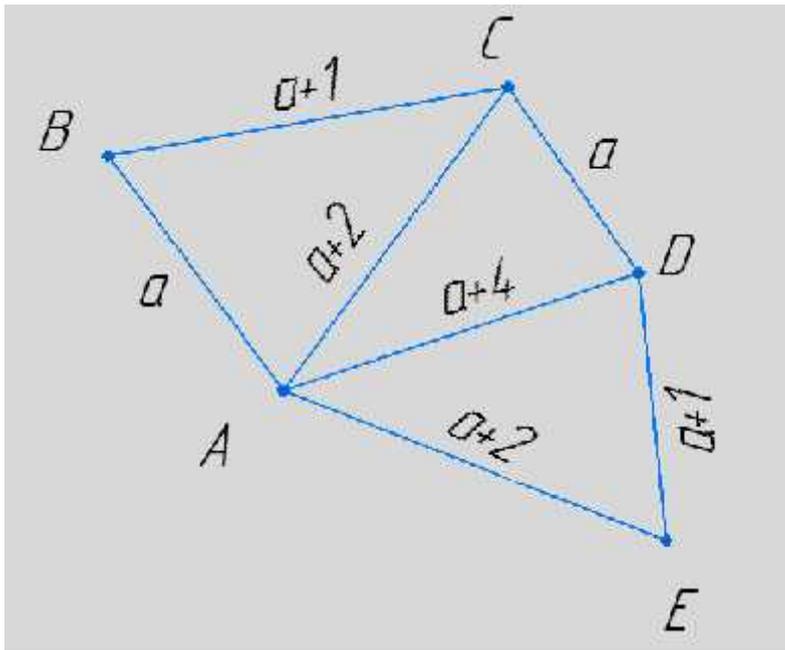


наименьшее расстояние - 24.
 Ответ: 2

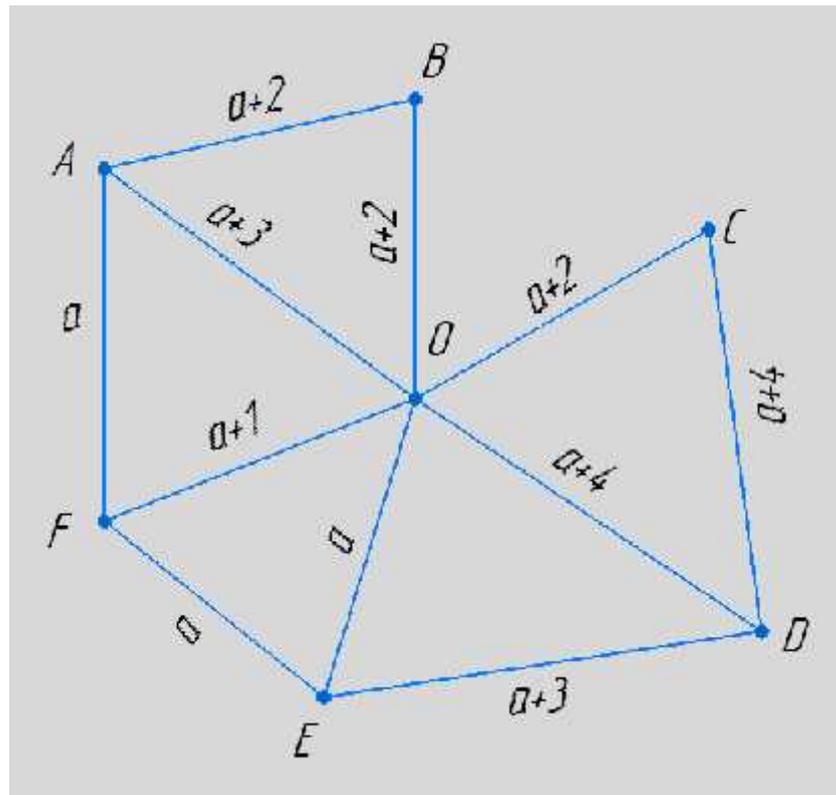
_____ :

(a) a

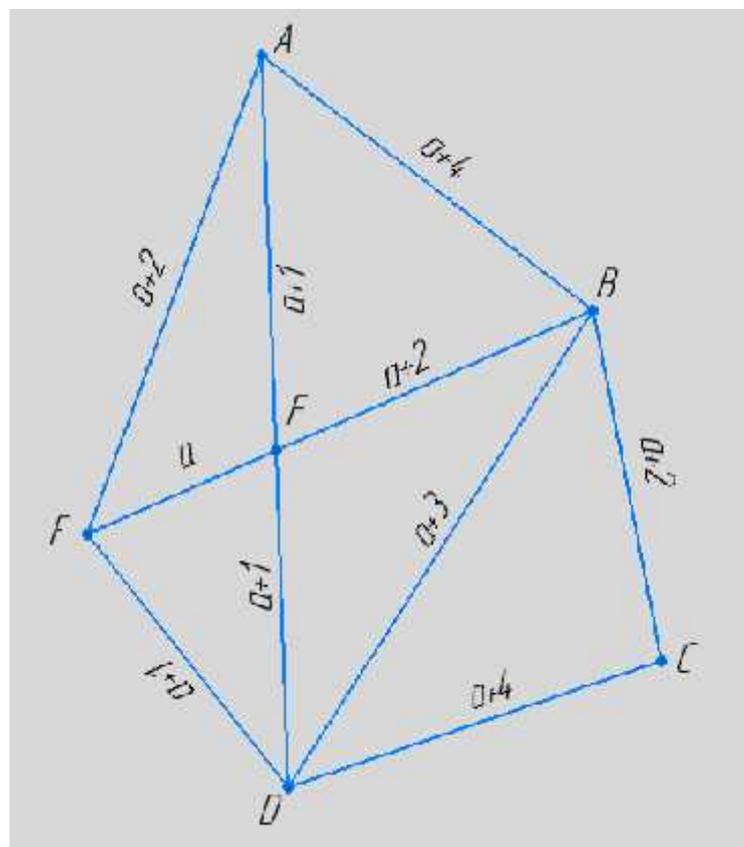
3



4



5



XIX

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P—

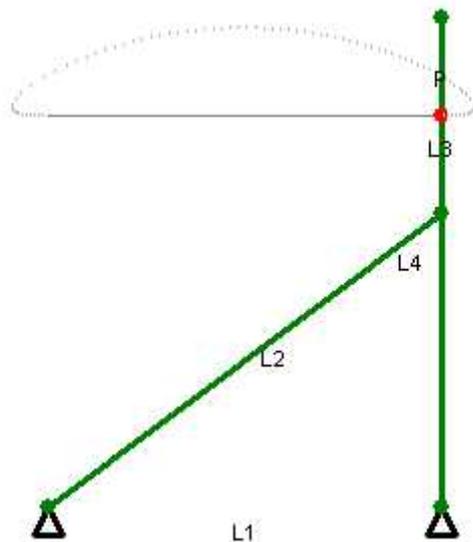
L₃,

_____. (L₁, L₂, L₃, L₄

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$$L_1 : L_2 : L_3 = 2 : 2.5 : 1 = 4 : 5 : 2.$$



.1

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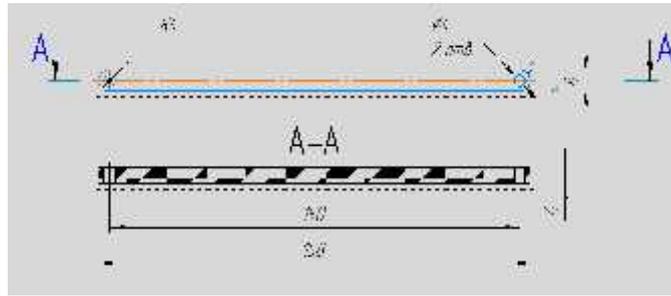
https://upload.wikimedia.org/wikipedia/commons/2/25/Chebyshev_linkage.gif

P

L₃,

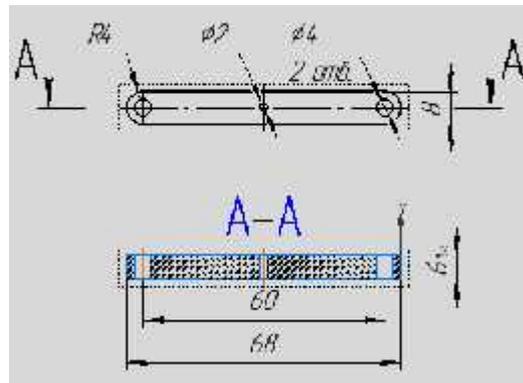
-3D.

1,



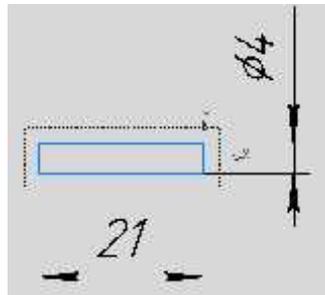
.2

$L_2 = L_4$



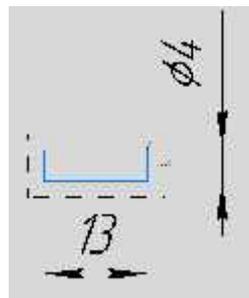
.3

L_3



.4

$l = 21.$



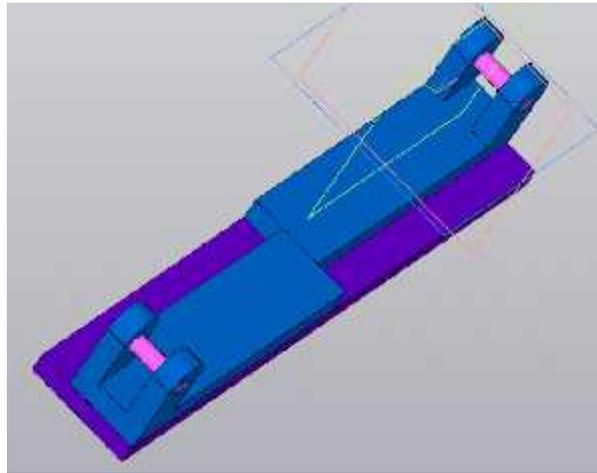
.5

$l = 13.$

L_1

$L_2 \quad L_4,$

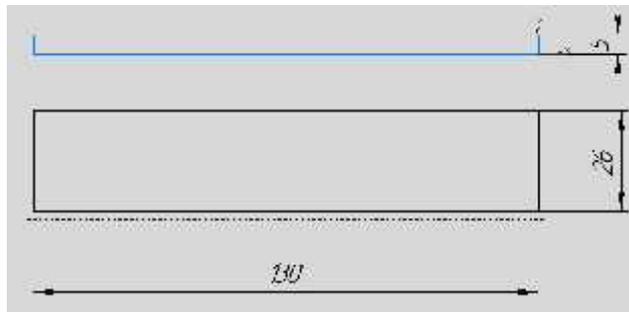
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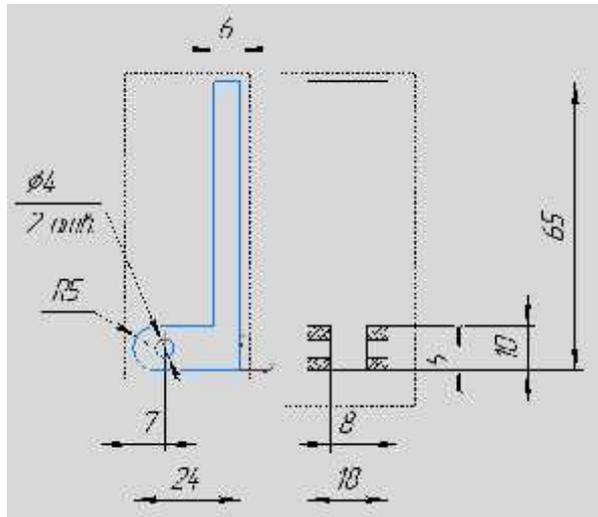
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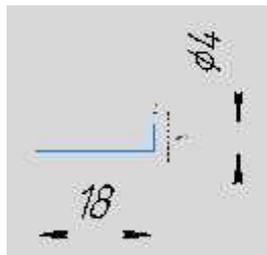
.7,8 9.



.7



.8



.9

$l=18.$

6.

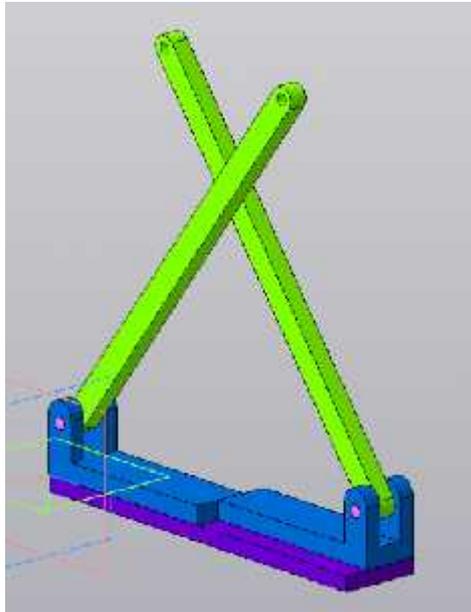
$$l=18.$$

(.6),

$L_2 (L_2 = L_4).$

« » « »,

(.10)

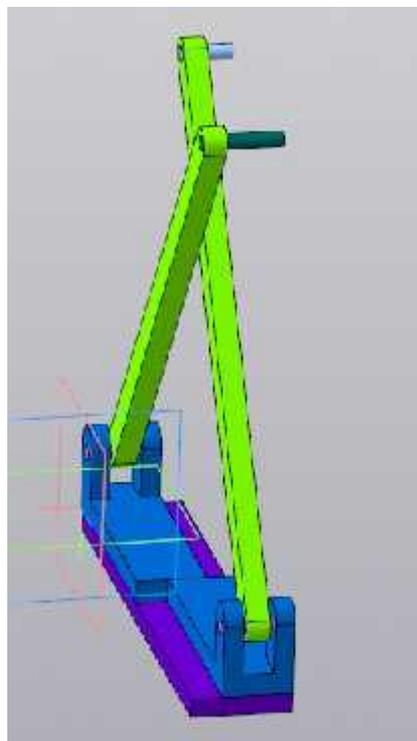


.10

$$l=21 \quad l=13.$$

« » « »,

(.11)

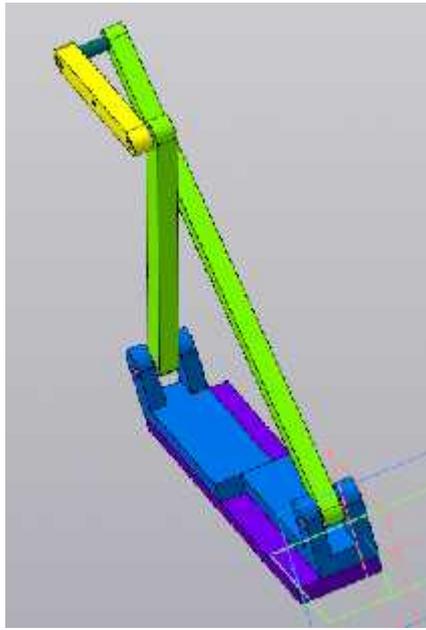


.11

$L_3 (.3).$

$$l=21 \quad l=13 (.12),$$

« » « ».

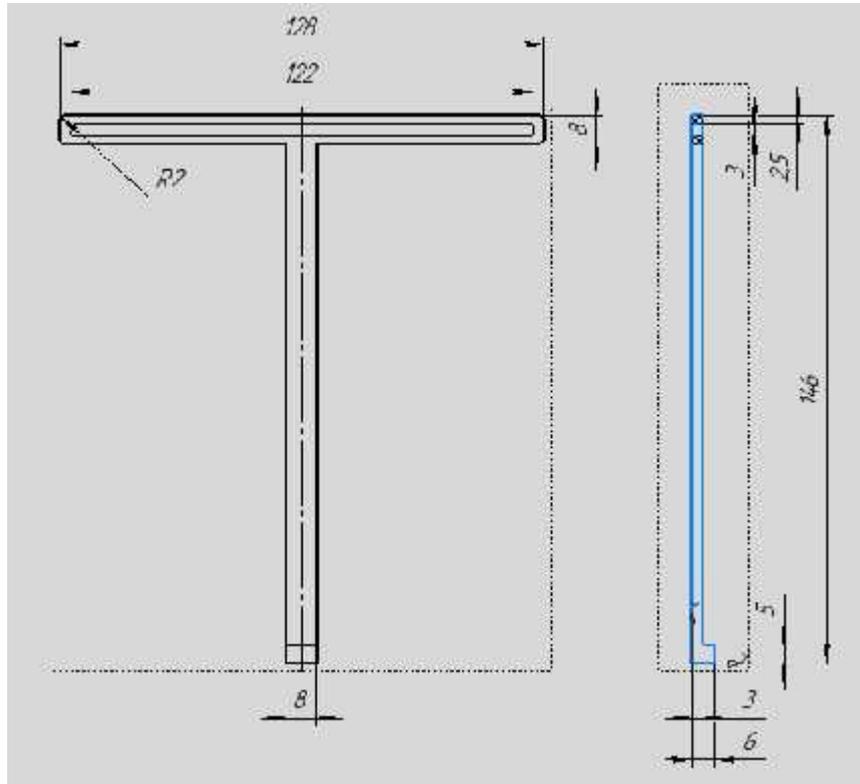


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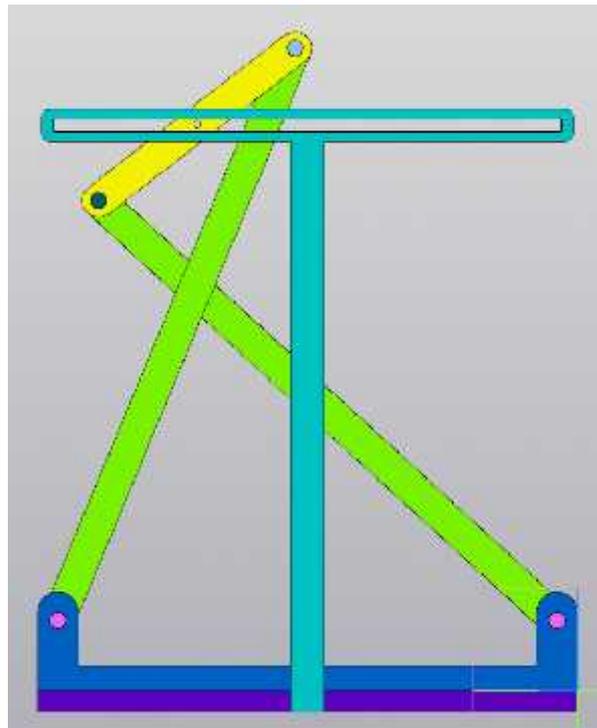
« »
L₃,

13.



. 13

« » (.14).



.14

a_1, a_2, \dots, a_m

$$y = f(x, a_1, a_2, \dots, a_m),$$

$$S = \sum_{i=1}^n (f(x, a_1, a_2, \dots, a_m) - y_i)^2$$

$$y = a \cdot x + b:$$

$$S = \sum_{i=1}^n ((a \cdot x_i + b) - y_i)^2$$

1.

$$y = a \cdot x + b,$$

1:

i	x_i	y_i	x_i^2	$x_i \cdot y_i$
1				
⋮				
n				
	$\sum x_i$	$\sum y_i$	$\sum x_i^2$	$\sum x_i \cdot y_i$

2.

b,

$$\begin{cases} a \cdot \sum_{i=1}^n x_i^2 + b \cdot \sum_{i=1}^n x_i = \sum_{i=1}^n x_i \cdot y_i \\ a \cdot \sum_{i=1}^n x_i + b \cdot n = \sum_{i=1}^n y_i \end{cases}$$

3.

b,

4.

b

5.

1	x	2.40	3.80	4.20	4.80	5.60	6.30	7.10	8.20
	y	3.52	4.64	4.96	5.44	6.08	6.64	7.28	8.16
2	x	1.70	2.80	3.50	4.30	5.80	6.70	6.90	7.80
	y	-0.19	1.24	2.15	3.19	5.14	6.31	6.57	7.74
3	x	0.80	1.30	1.80	2.30	2.70	3.80	4.60	5.50
	y	1.64	0.04	-1.56	-3.16	-4.44	-7.96	-10.52	-13.40
4	x	0.15	0.30	0.42	0.57	0.75	0.88	0.92	1.30
	y	-1.42	-1.05	-0.75	-0.37	0.075	0.40	0.50	1.45
5	x	2.70	3.50	4.60	5.10	5.80	6.30	7.20	7.90
	y	0.52	1.80	3.56	4.36	5.48	6.28	7.72	8.84
6	x	1.70	2.30	2.90	3.40	3.80	4.50	5.40	6.20
	y	5.39	5.81	6.23	6.58	6.86	7.35	7.98	8.54
7	x	2.60	3.20	3.80	4.50	5.70	6.30	6.90	7.50
	y	0.78	0.06	-0.66	-1.50	-2.94	-3.66	-4.38	-5.10
8	x	0.30	0.70	1.20	1.50	2.10	2.80	3.40	3.90
	y	-0.11	1.61	3.76	5.05	7.63	10.64	13.22	15.37
9	x	3.70	4.30	4.80	5.20	5.90	6.70	7.10	7.50
	y	5.34	7.26	8.86	10.14	12.38	14.94	16.22	17.50
10	x	1.10	1.60	1.90	2.30	2.80	3.20	3.70	4.10
	y	-3.95	-4.70	-5.15	-5.75	-6.50	-7.10	-7.85	-8.45
11	x	0.60	0.90	1.30	1.50	1.80	2.10	2.60	3.10
	y	2.60	3.81	5.07	6.15	7.32	8.49	10.44	12.39
12	x	0.30	0.42	0.56	0.75	0.83	0.90	0.93	0.97
	y	-0.86	-0.62	-0.13	0.40	0.62	0.82	0.90	1.016
13	x	1.20	1.70	1.90	2.10	2.60	2.90	3.20	3.50
	y	3.78	4.48	4.76	5.04	5.74	6.16	6.58	7.00

14	x	2.30	2.60	3.00	3.30	3.70	4.10	4.30	5.20
	y	-1.57	-2.14	-2.90	-3.47	-4.23	-4.99	-5.37	-7.08
15	x	1.30	1.90	2.40	2.90	3.50	4.20	4.70	5.10
	y	0.81	3.63	5.98	8.33	11.15	14.44	16.79	18.67
16	x	2.30	2.70	3.10	3.80	4.70	4.90	5.80	
	y	-3.80	-3.60	-3.50	-3.30	-3.00	-3.01	-2.80	
17	x	1.30	2.50	4.70	5.20	6.80	7.10	8.30	
	y	3.37	3.80	4.20	4.30	4.40	4.50	4.60	
18	x	1.70	3.20	4.10	4.90	5.70	6.80	9.10	
	y	-1.20	-0.40	-0.10	0.06	0.20	0.40	0.80	
19	x	2.10	2.80	3.60	5.10	5.90	7.20	8.30	
	y	-3.00	-2.30	-1.75	-0.90	-0.60	-0.16	-0.17	
20	x	1.10	2.40	3.20	4.70	5.00	5.80	7.30	
	y	2.60	2.90	3.00	3.10	3.16	3.20	3.30	
21	x	1.70	2.80	3.40	4.50	5.90	6.80	7.50	
	y	-4.40	-3.60	-3.30	-2.80	-2.40	-2.20	-2.00	
22	x	4.70	5.90	6.30	6.90	7.50	8.40	9.60	
	y	3.40	3.55	3.60	3.70	3.76	3.86	4.00	
23	x	1.80	2.50	3.70	4.20	5.40	6.20	7.10	
	y	-0.80	-0.40	0.10	0.30	0.60	0.80	1.00	
24	x	2.30	2.80	3.60	4.20	4.90	5.70	6.40	
	y	3.80	4.20	4.80	5.10	5.40	5.70	6.00	
25	x	4.10	4.70	5.30	6.10	7.20	8.30	9.10	
	y	-0.45	-0.10	0.10	0.46	0.80	1.20	1.40	
26	x	3.20	3.80	4.60	4.90	5.10	5.80	6.30	
	y	4.40	4.90	5.40	5.60	5.70	6.10	6.30	

27	x	4.20	4.90	5.30	5.80	6.40	7.50	8.20
	y	0.12	0.67	0.90	1.20	1.50	2.00	2.30
28	x	2.10	2.70	3.40	3.90	4.20	5.10	6.20
	y	5.10	6.05	6.90	7.40	7.70	8.50	9.20
29	x	3.10	3.70	4.50	5.30	6.80	7.10	7.90
	y	5.00	5.20	5.40	5.60	5.90	6.00	6.10
30	x	2.80	3.90	4.70	5.40	6.30	6.90	7.50
	y	2.30	3.60	4.30	4.90	5.50	5.80	6.20
31	x	3.20	4.10	4.80	5.30	6.40	7.30	8.10
	y	3.50	3.80	4.00	4.10	4.36	4.50	4.70
32	x	2.30	3.40	4.70	5.40	6.20	7.80	8.20
	y	3.90	4.56	5.20	5.50	5.80	6.40	6.50